

# The Subgroups of $S_4$

order of subgroup

conjugacy classes

$A_4$	$D_4$	$S_3$
$Z_4$	$V$	$V$
$Z_3$	$Z_2$	$Z_2$

24

$S_4$

12

$A_4$

8

$\langle(1\ 2\ 3\ 4), (1\ 3)\rangle$      $\langle(1\ 2\ 4\ 3), (1\ 4)\rangle$      $\langle(1\ 3\ 2\ 4), (1\ 2)\rangle$

6

$\langle(1\ 2\ 3), (1\ 2)\rangle$      $\langle(1\ 2\ 4), (1\ 2)\rangle$      $\langle(1\ 3\ 4), (1\ 3)\rangle$      $\langle(2\ 3\ 4), (2\ 3)\rangle$

4

$\langle(1\ 2\ 3\ 4)\rangle$      $\langle(1\ 2\ 4\ 3)\rangle$      $\langle(1\ 3\ 2\ 4)\rangle$

$\langle(1\ 3), (2\ 4)\rangle$      $\langle(1\ 4), (2\ 3)\rangle$      $\langle(1\ 2), (3\ 4)\rangle$

$\langle(1\ 2)(3\ 4), (1\ 3)(2\ 4)\rangle$

3

$\langle(1\ 2\ 3)\rangle$      $\langle(1\ 2\ 4)\rangle$      $\langle(1\ 3\ 4)\rangle$      $\langle(2\ 3\ 4)\rangle$

2

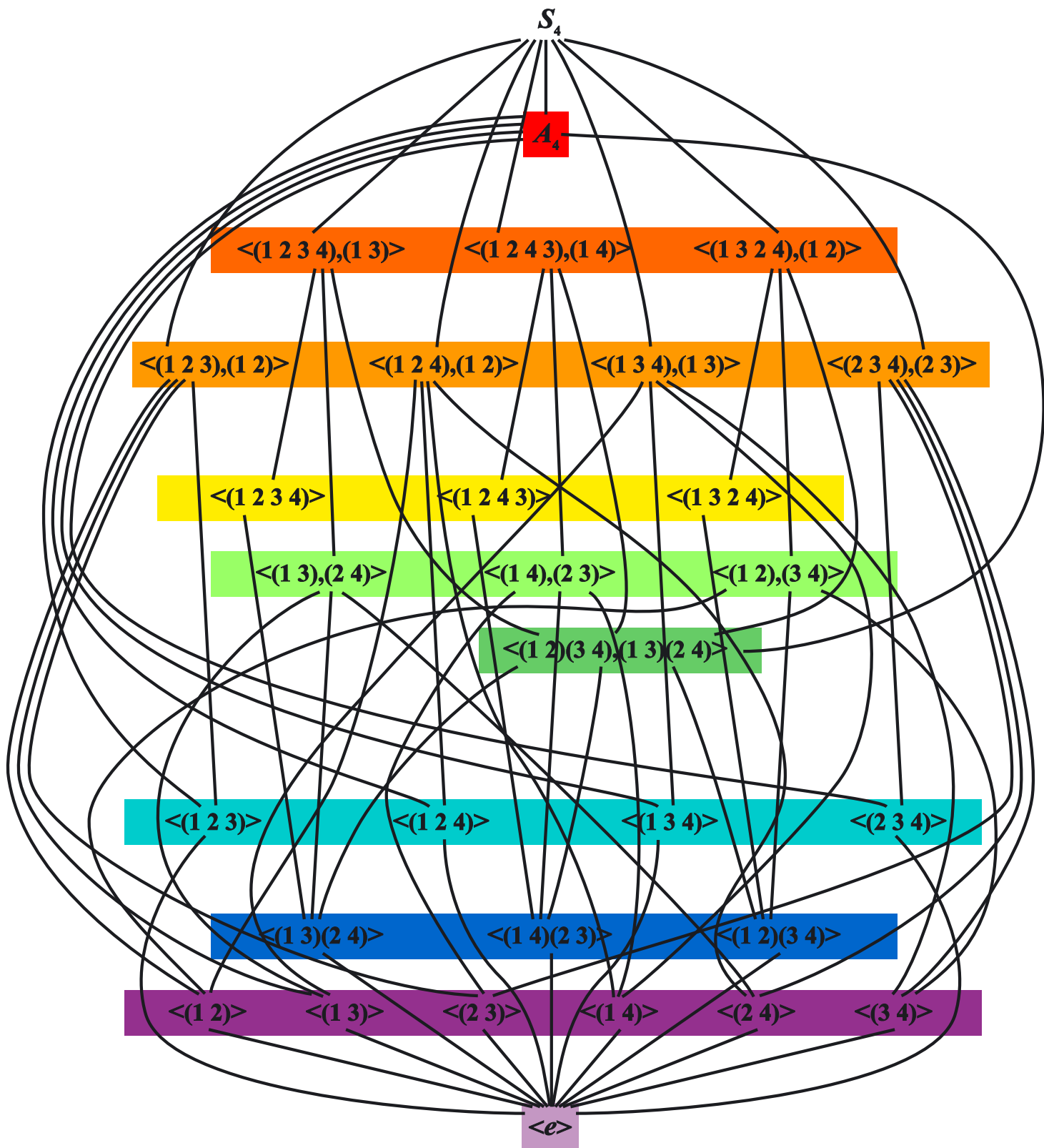
$\langle(1\ 3)(2\ 4)\rangle$      $\langle(1\ 4)(2\ 3)\rangle$      $\langle(1\ 2)(3\ 4)\rangle$

$\langle(1\ 2)\rangle$      $\langle(1\ 3)\rangle$      $\langle(2\ 3)\rangle$      $\langle(1\ 4)\rangle$      $\langle(2\ 4)\rangle$      $\langle(3\ 4)\rangle$

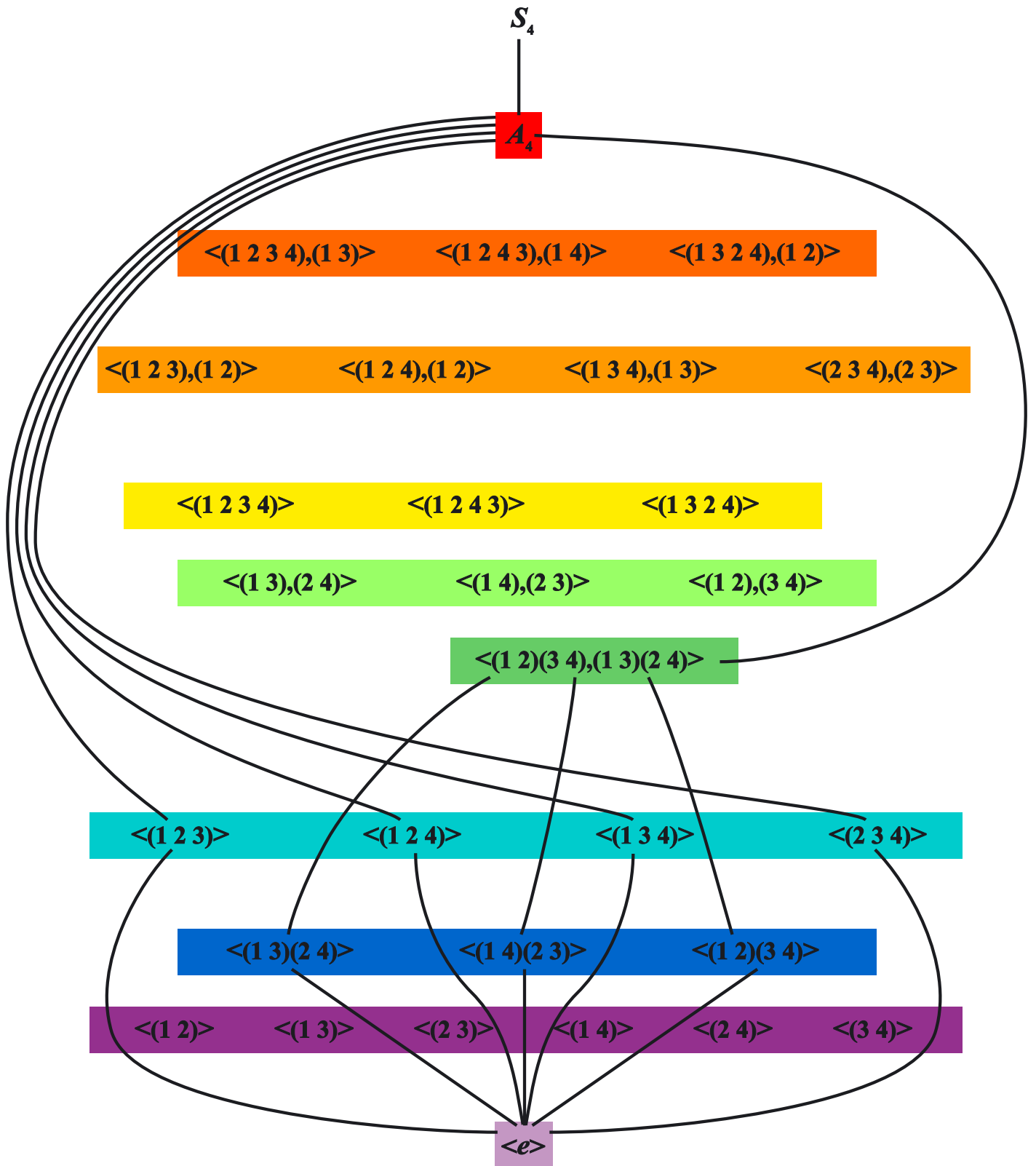
1

$\langle e \rangle$

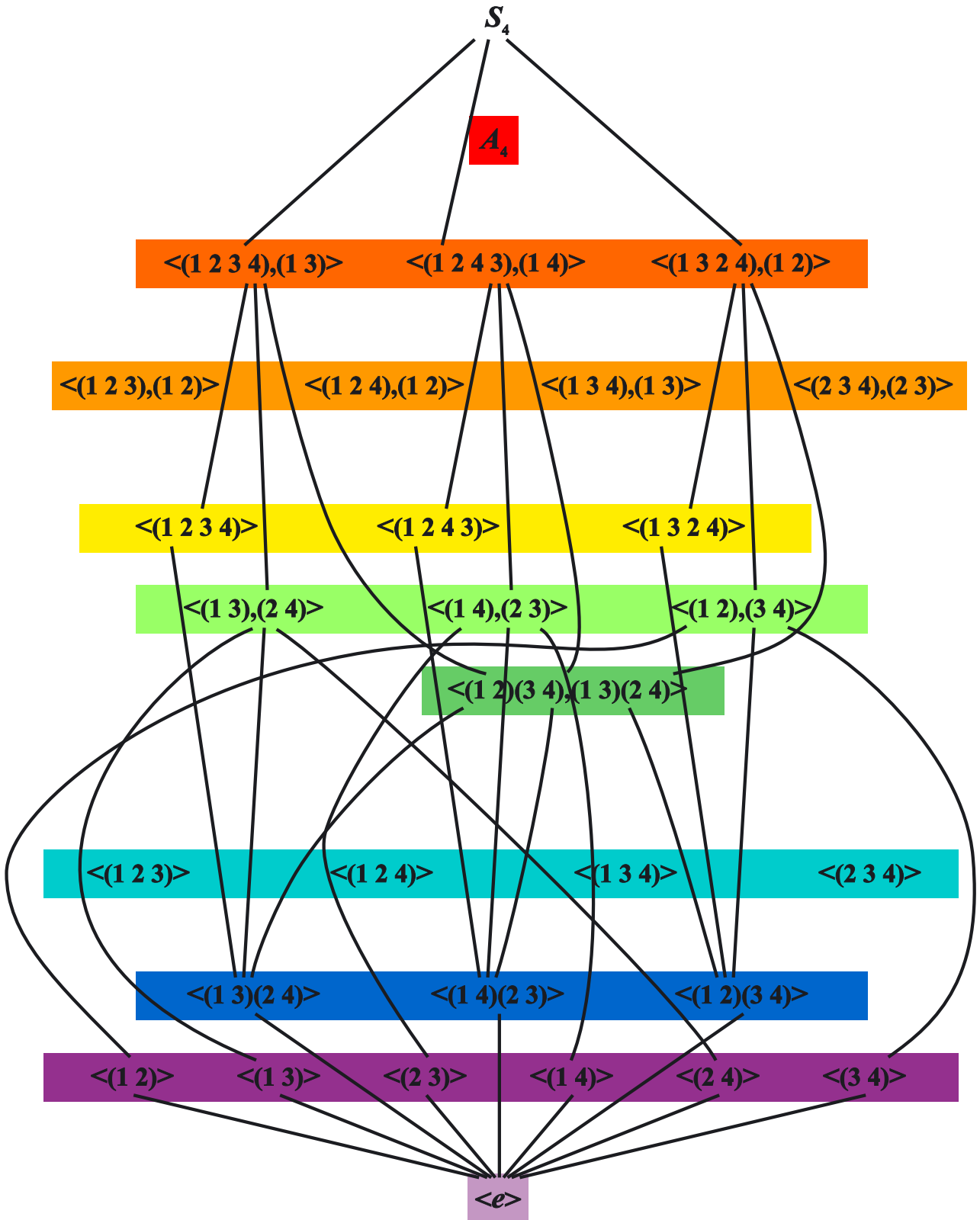
# Full Subgroup Diagram



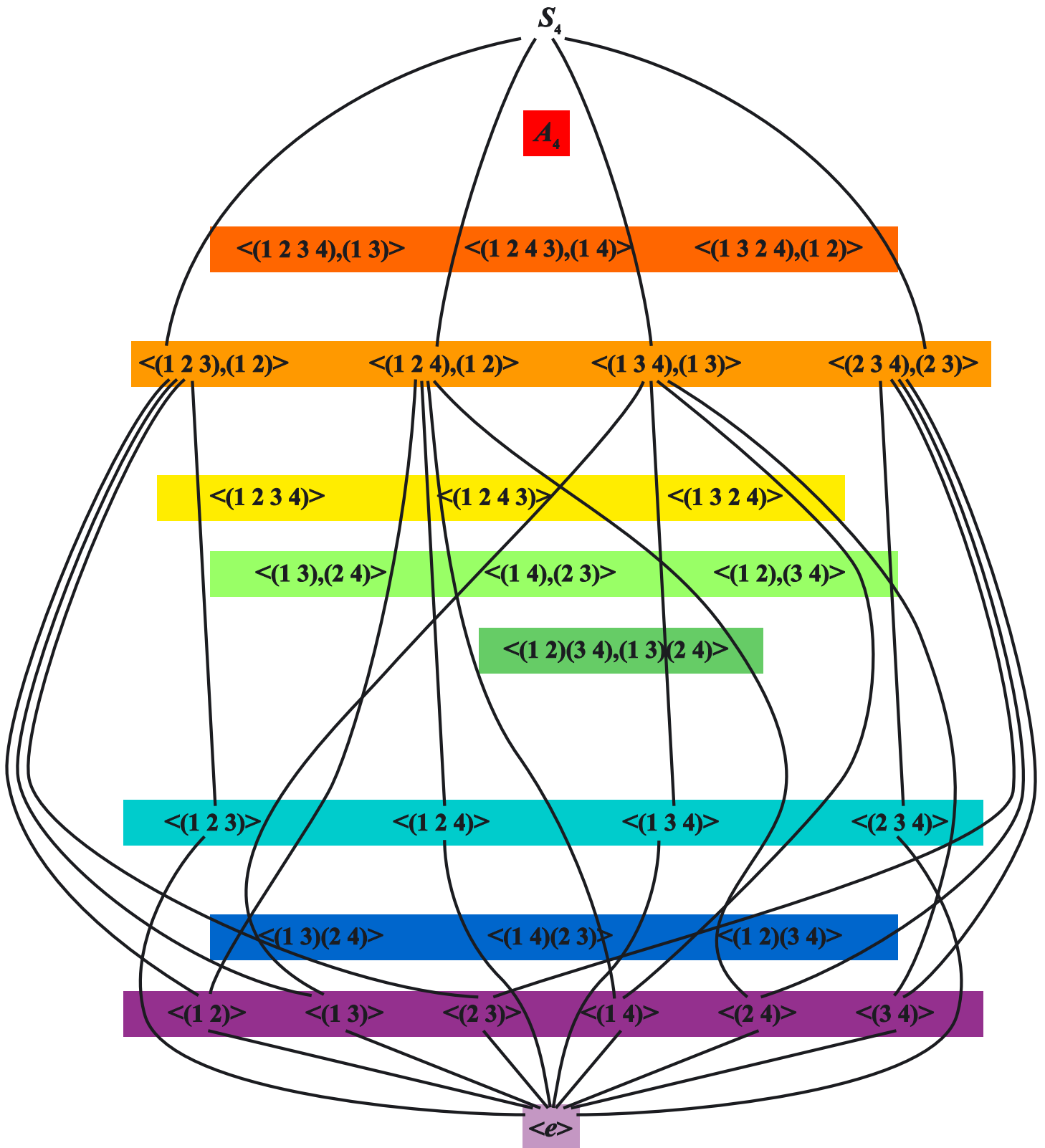
# Links Through $A_4$



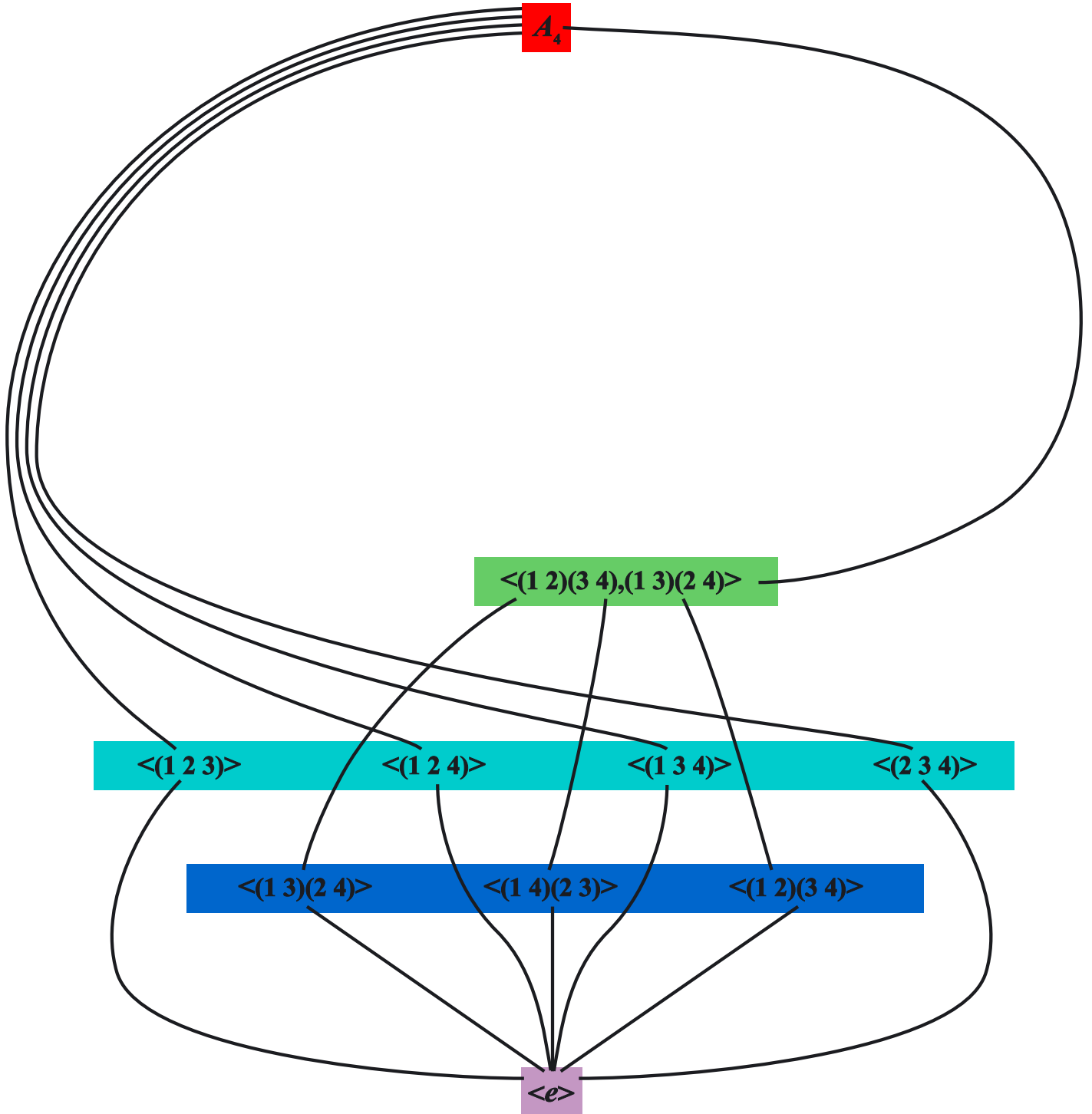
# Links Through $D_4$



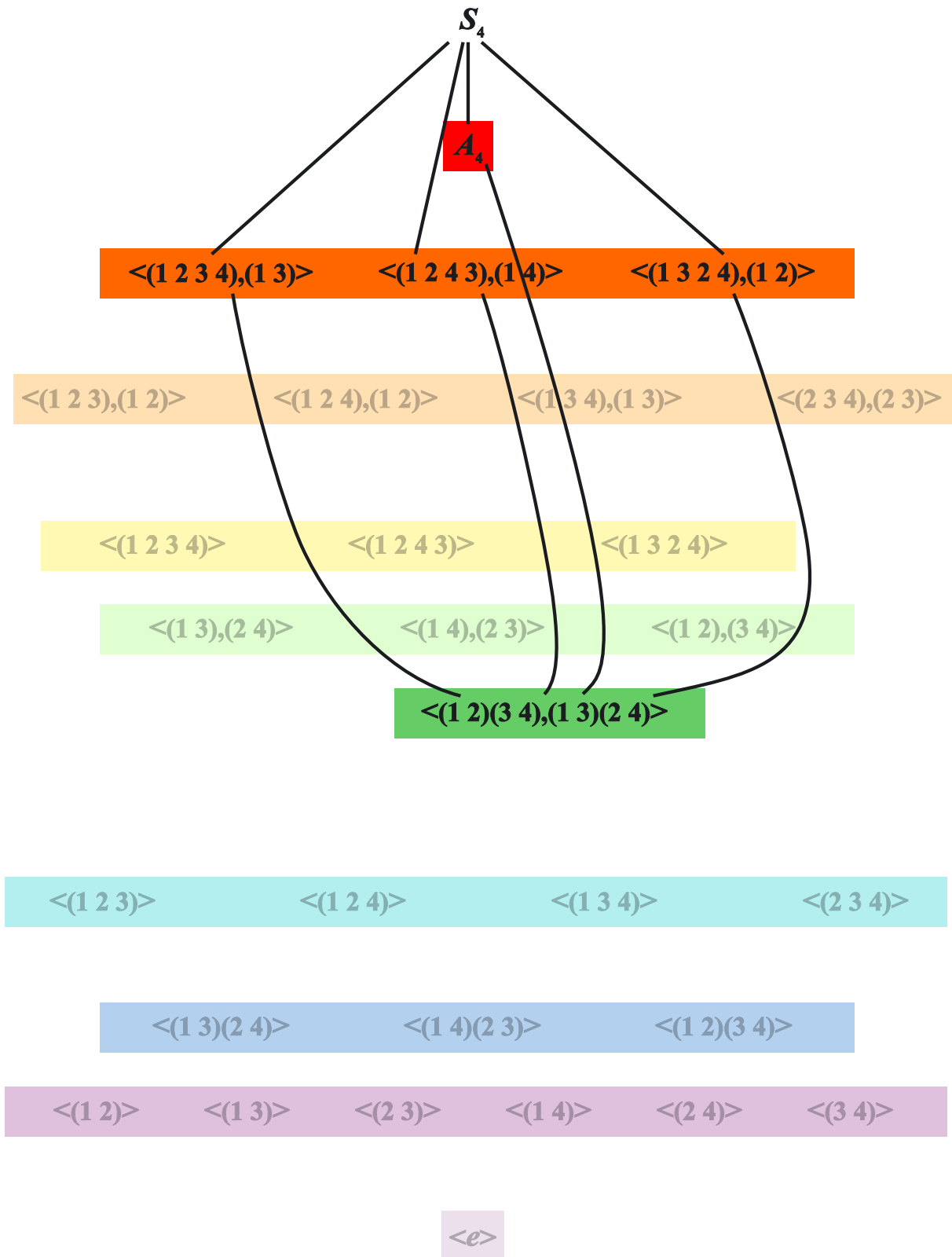
# Links Through $S_3$



$A_4$  subgroup diagram



# Subgroups containing the normal copy of $V$





Isomorphism Theorems: Comparison to subgroups of  $S_3 \cong S_4/V$

