## MATH 391

## Putnam Seminar

## Cognitive Control:

What am I doing? Why am I doing it? How will it help me?
Problem-solve away from frustration. Don't give up.
Heuristics: Search for a pattern. Draw a figure. Choose effective notation. Work backward. Use pigeonhole. Consider Modular Arithmetic. $n$ is for Induction.
New Problems:

1. How many zeroes does $1,000,000$ ! (one million factorial) end in?
2. Show that the product of $n$ successive integers is always divisible by $n$ !.
3. Let $f(x)$ be a polynomial of degree $n$ such that

$$
f(k)=\frac{k}{k+1}
$$

for each $k=0,1,2, \ldots, n$. What is the value of $f(n+1)$ ?
4. Decide whether or not a cube can be decomposed into a finite number of smaller cubes, all of different sizes.

