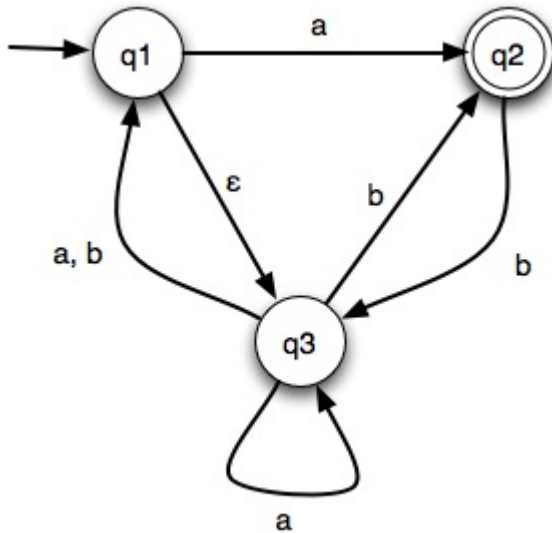


Assume that $\Sigma = \{0, 1\}$ unless otherwise noted.

1. Give the RE, NFA, and DFA for the language $A = \{w \mid w \text{ contains an even number of 0s, or contains exactly two 1s}\}$. The NFA can have at most six states.
2. Is the language over $\Sigma = \{a, b, c\}$ containing at least one a and at least one b regular? Prove it.
3. Prove that the language $D = \{a^n b^n c^i \mid n \leq i \leq 2n\}$ is not regular.
4. Provide the DFA for the language that is the set of all strings of 0s and 1s whose number of 0s is divisible by 4 and the number of 1s is even. Convert that DFA to an RE using the GNFA method.
5. Convert this NFA to a DFA:



6. Show that the class of regular languages is closed under union, concatenation, and Kleene star.
7. For languages A and B, let the shuffle of A and B be the language

$$\{w \mid w = a_1 b_1 \cdots a_k b_k, \text{ where } a_1 \cdots a_k \in A \text{ and } b_1 \cdots b_k \in B, \text{ each } a_i, b_i \in \Sigma^*\}.$$

Show that the class of regular languages is closed under shuffle.