COSC 440 – Theory of Computation Exam #1 Review Questions Fall 2008

1.) Is the language $\{w \mid where w \text{ has as a substring } 01\}$ regular? Prove it.

2.) Give the DFA for the set of strings that either begin or end (or both) with 01. Give the formal definition of the DFA in addition to the state diagram.

3.) Is the language $\{w \mid w = w^R\}$ (w is a palindrome) regular? Prove it.

4.) Give the NFA, DFA and RE for the set of strings over the alphabet $\{0, 1, ..., 9\}$ such that the final digit has appeared before.

5.) Convert the following CFG to CNF:

 $\begin{array}{l} S \mathrel{\rightarrow} AB \\ A \mathrel{\rightarrow} aAA \mid \epsilon \\ B \mathrel{\rightarrow} bBB \mid \epsilon \end{array}$

6.) Give a CFG for the language $\{w \mid w \text{ has twice as many 0's as 1's}\}$.

7.) Give the PDA for the language $\{w \mid w \text{ has twice as many 0's as 1's}\}$.

8.) Is the language $\{a^m b^n c^n \mid m, n \ge 0\}$ regular or context free? Prove it.

9.) Prove that the language $\{a^i b^j c^k \mid i != j \text{ or } j != k\}$ is either context free or not context free.

10.) Show that the language $\{0^n \# 0^{2n} \# 0^{3n} \mid n \ge 0\}$ is not context free.