COSC 440 - Theory of Computation
Exam \#1 Review Questions
Fall 2008
1.) Is the language $\{\mathrm{w} \mid$ where w has as a substring 01$\}$ regular? Prove it.
2.) Give the DFA for the set of strings that either begin or end (or both) with 01 . Give the formal definition of the DFA in addition to the state diagram.
3.) Is the language $\left\{w \mid w=w^{R}\right\}$ (w is a palindrome) regular? Prove it.
4.) Give the NFA, DFA and RE for the set of strings over the alphabet $\{0,1, \ldots, 9\}$ such that the final digit has appeared before.
5.) Convert the following CFG to CNF:

$$
\begin{aligned}
& \mathrm{S}->\mathrm{AB} \\
& \mathrm{~A}->\mathrm{aAA} \mid \varepsilon \\
& \mathrm{B}->\mathrm{bBB} \mid \varepsilon
\end{aligned}
$$

6.) Give a CFG for the language $\{\mathrm{w} \mid \mathrm{w}$ has twice as many 0 's as 1 's $\}$.
7.) Give the PDA for the language $\{\mathrm{w} \mid \mathrm{w}$ has twice as many 0 's as 1 ' s$\}$.
8.) Is the language $\left\{a^{m} b^{n} c^{n} \mid m, n>=0\right\}$ regular or context free? Prove it.
9.) Prove that the language $\left\{a^{i} b^{j} c^{k} \mid i!=j\right.$ or $\left.j!=k\right\}$ is either context free or not context free.
10.) Show that the language $\left\{0^{\mathrm{n}} \# 0^{2 \mathrm{n}} \# 0^{3 \mathrm{n}} \mid \mathrm{n}>=0\right\}$ is not context free.

